

New Method for Opacity Correction
in
Oversampled Volume Ray Casting

Jong Kwan Lee and Timothy S. Newman

Department of Computer Science
University of Alabama in Huntsville
U. S. A.

CONTENTS

❖ Introduction

- DVR: (Oversampled) Ray Casting
- Objective

❖ Related Work

❖ New Opacity Correction Approach

❖ Experimental Results

❖ Conclusion

INTRODUCTION

❖ Volume Ray Casting

- Direct volume rendering (DVR)
- Composite samples (F-to-B or B-to-F)
- # samples $>$ Nyquist sampling freq.

❖ Oversampled Ray Casting

- Multiple samples within a voxel
 - over-composited opacity
- Objective
 - Correct opacity to avoid artifacts from over-composited opacity

RELATED WORK

❖ Lichtenbelt et al. [2]:

➤ Assumption: homogeneous datasets

➤ Motivated by Lacroute [1]

➤ $\alpha' = 1 - \sqrt[N]{1 - \alpha}$ (1)

N : oversampling factor, α : original opacity, α' : corrected opacity

❖ Lacroute [1]:

➤ Opacity formula in terms of sampling spacing

➤ Equivalent to Equation (1)

❖ [1,2]'s opacity correction is used in [3, 4]

[1] P. Lacroute, *Fast Volume Rendering Using a Shear-Warp Factorization of the Viewing Transformation*, Doctoral Dissertation (Technique Report CSL-TR-95-678), Stanford University, 1995.

[2] B. Lichtenbelt, R. Crane, and S. Naqvi, *Introduction to Volume Rendering*, Prentice Hall, Upper Saddle River, NJ, 1998.

[3] J. P. Schulze, M. Kraus, U. Lang, and T. Ertl, "Integrating Pre-Integration into the Shear-Warp Algorithm," *Proc., Third Int'l Workshop on Volume Graphics*, Tokyo, pp. 109-118, July, 2003.

[4] M. Weiler, R. Westermann, C. Hansen, K. Zimmerman, and T. Ertl, "Level-Of-Detail Volume Rendering via 3D Textures," *Proc., 2000 IEEE Symp. On Volume Visualization*, Salt Lake City, pp. 7-13, 2000.

NEW OPACITY CORRECTION APPROACH

- ❖ Generalize **derivation** of Equation (1)
- ❖ No homogeneity assumption
- ❖ E.g., Composited transparency

for oversampling x2 within a voxel:

$$\triangleright (1 - \alpha_{u1}) = (1 - p\alpha_{o1}) \times (1 - p\alpha_{o2}), \text{ where}$$

α : opacity, u, o : unit- & over- sampling

$$\text{Rearranging } \rightarrow F : (\alpha_{o1}\alpha_{o2})p^2 - (\alpha_{o1} + \alpha_{o2})p + \alpha_{o1} = 0.$$

$$(\alpha_{u1} = \alpha_{o1})$$

NEW CORRECTION

❖ Generalization

$$\begin{aligned}
 & (-1)^0 \left(\prod_{s=1}^N \alpha_{os} \right) p^N + (-1)^1 \left\{ \sum_{t=1}^N \left(\prod_{s=1, s \neq t}^N \alpha_{os} \right) \right\} p^{N-1} \\
 & + (-1)^2 \left\{ \sum_{u=1}^{N-1} \sum_{t=u+1}^N \left(\prod_{s=1, s \neq t, u}^N \alpha_{os} \right) \right\} p^{N-2} + (-1)^3 \left\{ \sum_{v=1}^{N-2} \sum_{u=v+1}^{N-1} \sum_{t=u+1}^N \left(\prod_{s=1, s \neq t, u, v}^N \alpha_{os} \right) \right\} p^{N-3} \\
 & + \dots + (-1)^N \alpha_{o1} p^0 = 0
 \end{aligned}$$

❖ Solve for p ($0 \leq p \leq 1$): new correction factor

❖ Accelerate computation via deg. 2 poly. fitting

➤ Approximation: $\hat{F}(p) = A \times p^2 + B \times p + C$

➤ Passing through $p_0 = 0.0$, $p_1 = 0.5$, $p_2 = 1.0$.

New Opacity Correction Approach

❖ Computational advantages

- Avoid $\sqrt[N]{1 - \alpha}$ operations
- Multiple use of new correction factor, p
- Reuse of inverse matrix

EXPERIMENTS

❖ Synthetic Data-Testing All Combination

❖ Real Data Tests (x5)

✓ Rendering Quality, Rendering Time

EXPERIMENTAL RESULTS I

COMPARISONS OVER ALL POSSIBLE COMBINATIONS OF SAMPLE VALUES (x2)

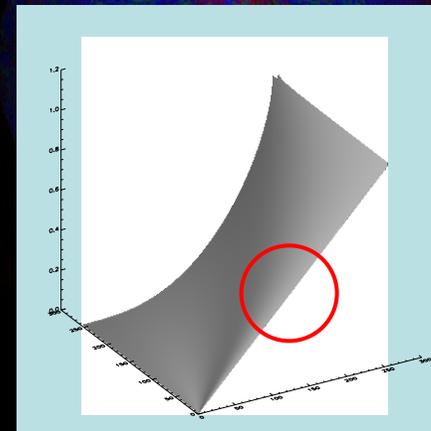
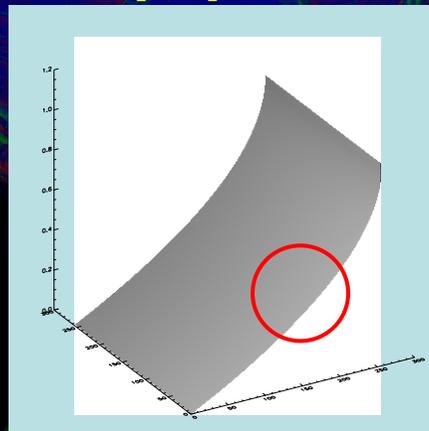
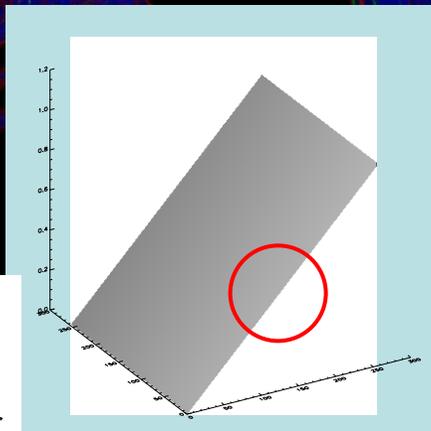
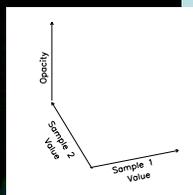
* SYNTHETIC DATA *

no correction

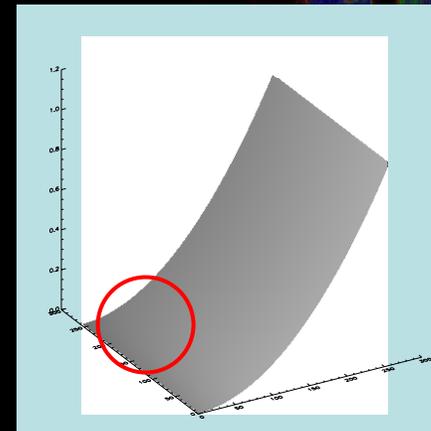
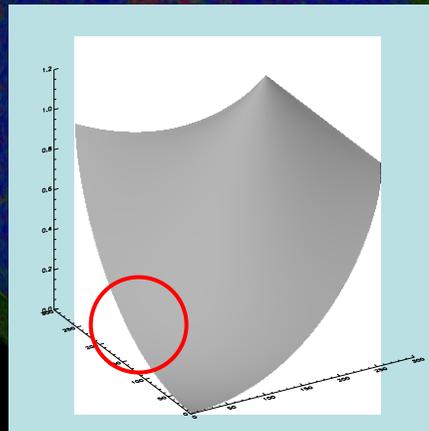
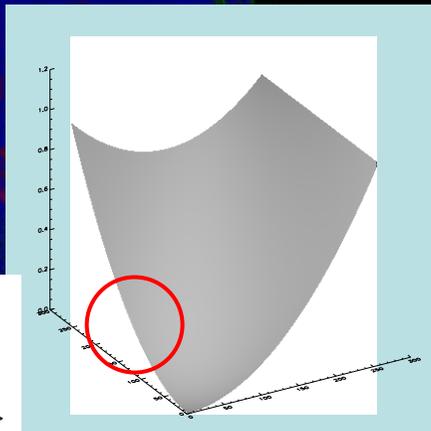
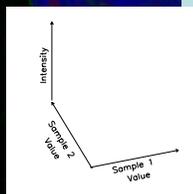
w/ [1, 2] correction

w/ new correction

RESULTANT
OPACITY



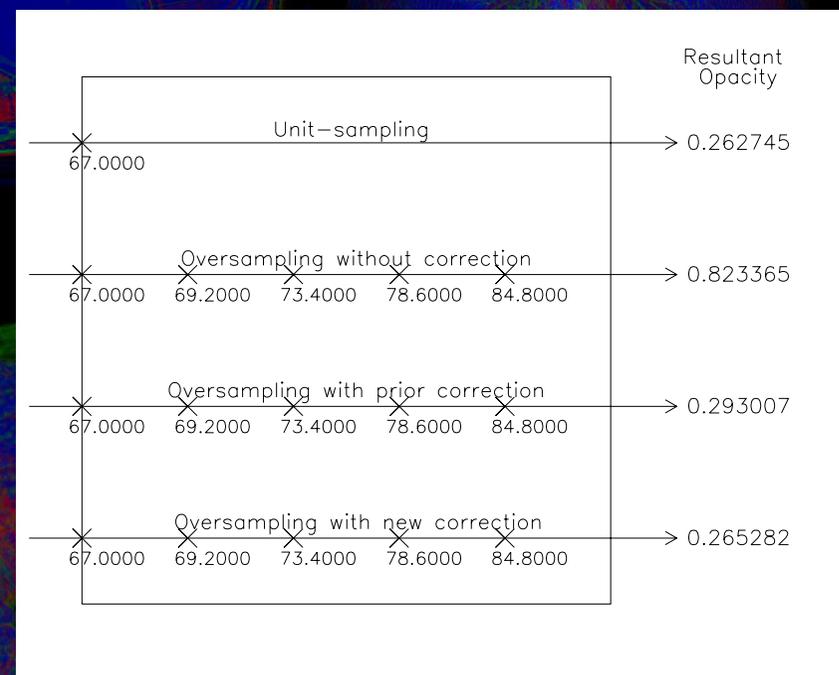
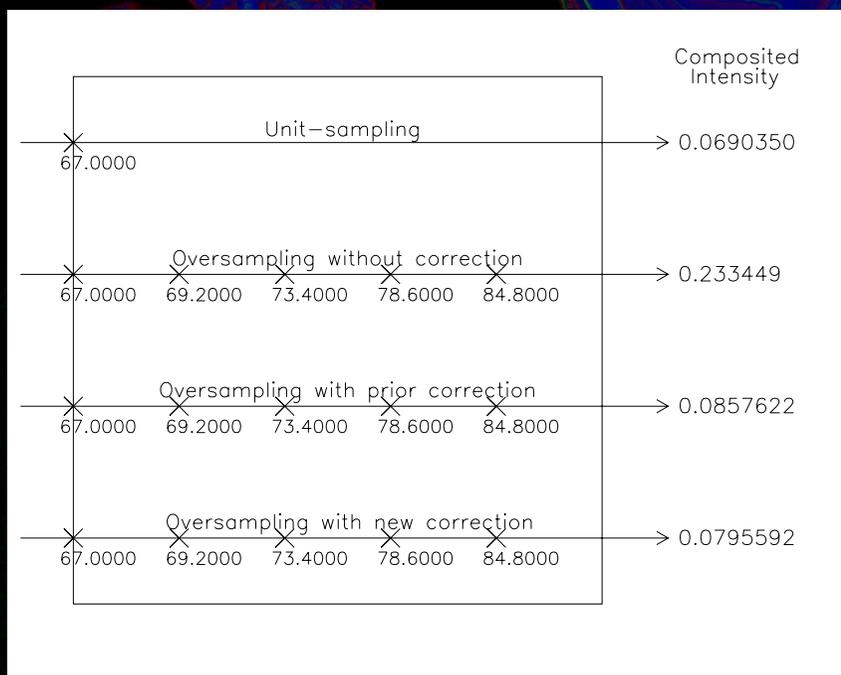
COMPOSITED
INTENSITY



EXPERIMENTAL RESULTS II

COMPARISON OF COMPOSITED OPACITIES & INTENSITIES FOR A VOXEL

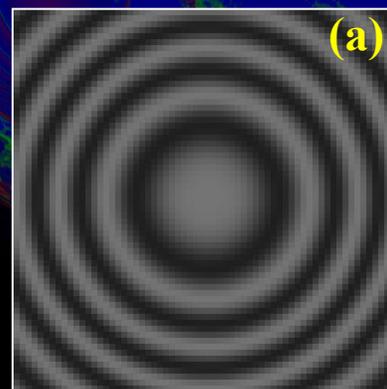
* AN EXAMPLE *



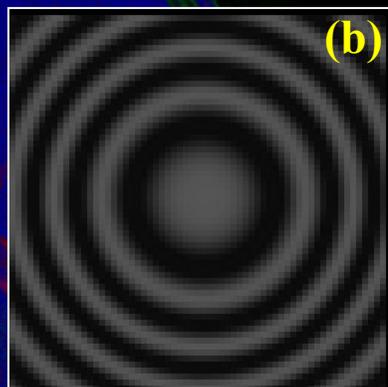
An example of comparison of composited intensities & resultant opacities for a voxel: Rays within a voxel for unit-sampling, oversampling without correction, oversampling with [1,2]'s correction, and oversampling with new correction from top to bottom, respectively

EXPERIMENTAL RESULTS III

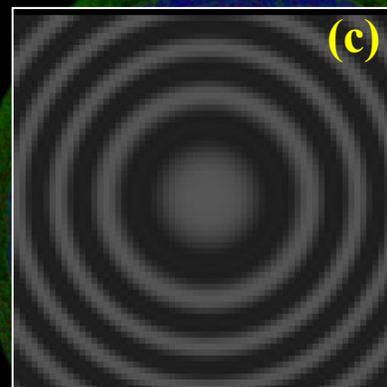
* COMPARISON vs. BENCHMARK *



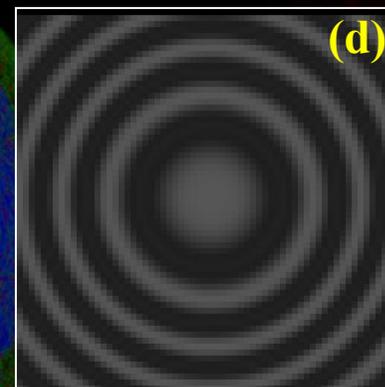
(a)



(b)



(c)



(d)

Marschner-Lobb dataset renderings (64x64x64) from (a) analytical integration and (b-d) oversampling (5 times) volume ray casting, (b) without opacity correction, (c) with [1,2]'s correction (d) with new opacity correction

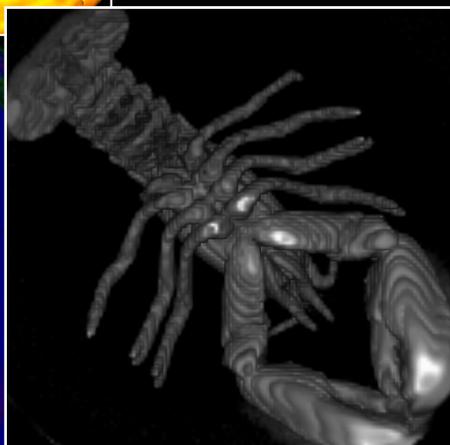
COMPARISON RENDERINGS I



(a)



(c)



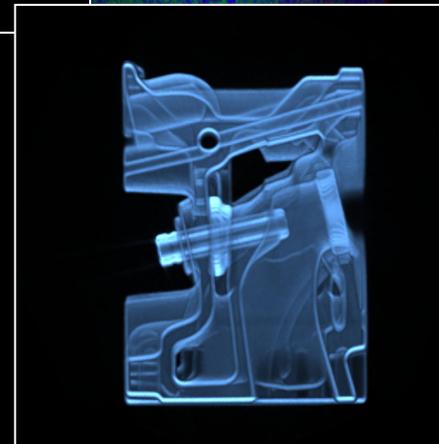
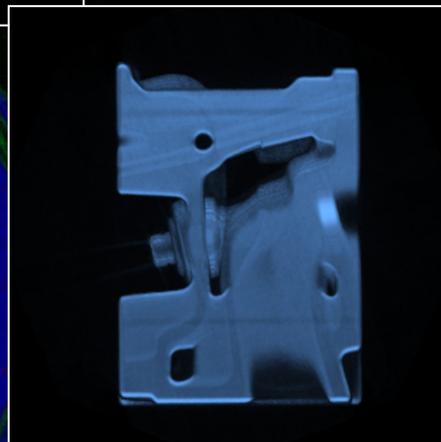
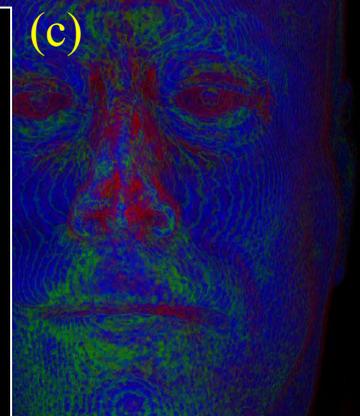
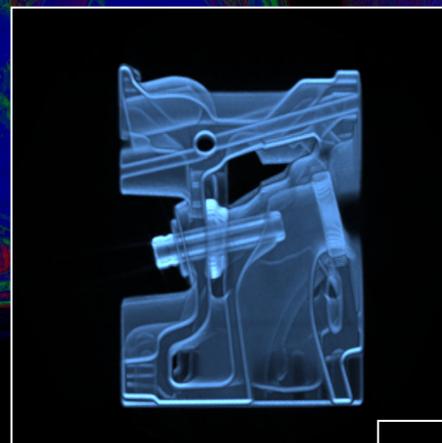
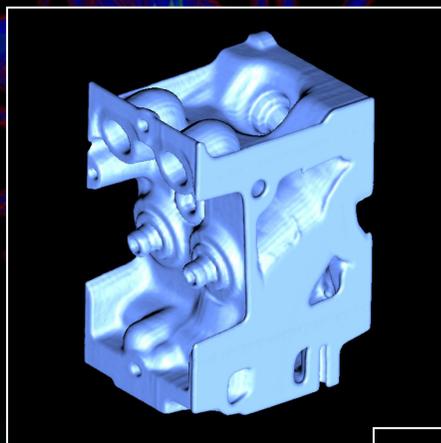
(b)



(d)

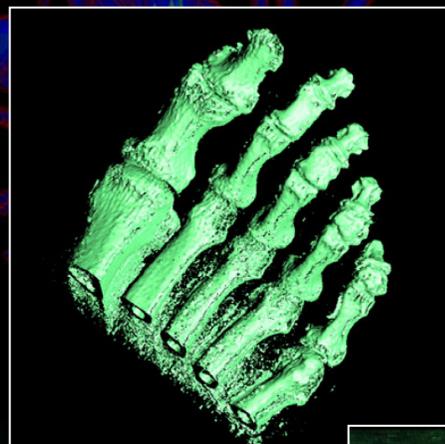
Lobster renderings (120x120x34, CT) from (a) Marching Cubes isosurfacing and (b-d) oversampling (5 times) volume ray casting, (b) without opacity correction, (c) with [1,2]'s correction (d) with new opacity correction

COMPARISON RENDERINGS II

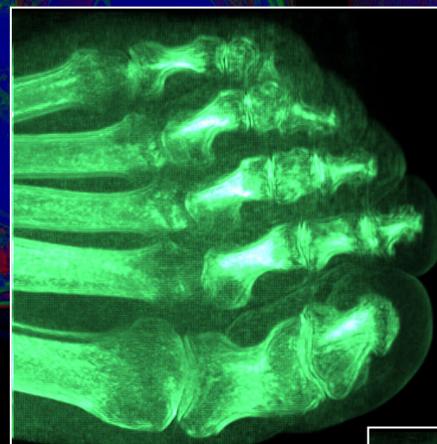


Engine block renderings (256x256x256, CT) from (a) Marching Cubes isosurfacing and (b-d) oversampling (5 times) volume ray casting, (b) without opacity correction, (c) with [1,2]'s correction (d) with new opacity correction

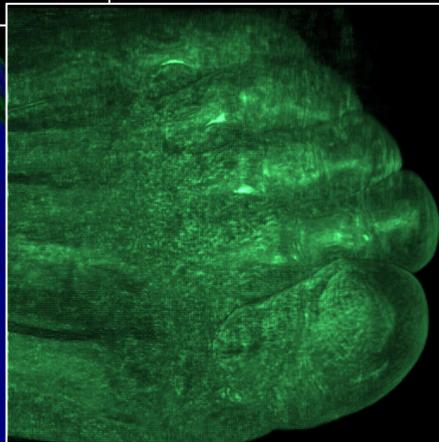
COMPARISON RENDERINGS III



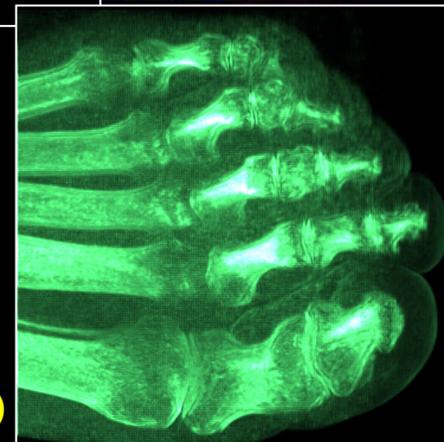
(a)



(c)



(b)



(d)

Foot renderings (256x256x256, CT) from (a) Marching Cubes isosurfacing and (b-d) oversampling (5 times) volume ray casting, (b) without opacity correction, (c) with [1,2]'s correction (d) with new opacity correction

APPROXIMATION ERROR

*Fitting Error, New Opacity Correction,
Lobster Dataset (120x120x34, CT)*

Fitting Error	Avg.	Std. Dev.	> 0.1
x5 Oversampling	0.0031	0.011	0.088%

PROCESSING TIME

Opacity Correction Speedup

New opacity correction vs. [1,2]'s correction for 40 real datasets

x5 oversampling	Max.	Avg.	Min.
Speedup	14.7	12.4	6.8

Overall VRC Rendering Speedup

New opacity correction vs. [1,2]'s correction for 40 real datasets

x5 oversampling	Max.	Avg.	Min.
Speedup	2.00	1.85	1.77

CONCLUSION

- ❖ New opacity correction
 - Generalization of existing opacity correction
 - ✓ Similar rendering quality
 - ✓ Faster rendering (~2 times overall)
 - No dataset homogeneity assumption
- ❖ Future work:
 - Even faster opacity correction?
 - Better accuracy?